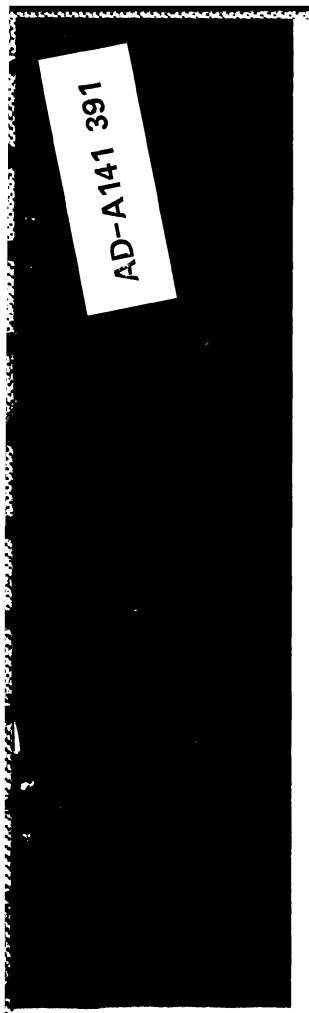


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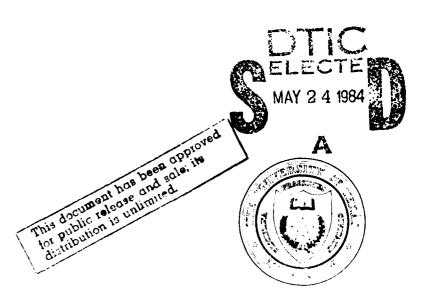
A NONLINEAR CONGESTION NETWORK MODEL FOR PLANNING INTERNAL MOVEMENT IN THE HAJJ

by

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- S. Duffuaa
- A. Yafi

CENTER FOR CYBERNETIC STUDIES

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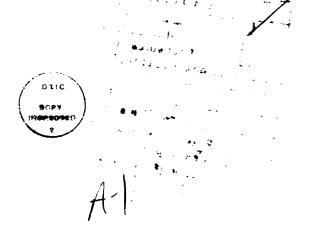
ABSTRACT

This paper develops a non-linear dynamic capacitated network model for planning the movements of pilgrims in the Hajj, one of the world's largest mass movements, according to religious ritual, which would assist in minimizing traffic congestion and the overcrowding of the holy sites. A new non-linear representation of congestion with convenient mathematical properties is made. The model is effective in producing quantitative and qualitative background for general policy decisions on the Hajj transportation.

KEY WORDS

Policy analysis

Non-linear dynamic capacitated network model
Goal programming
Hajj Pilgrimage
Nonlinear congestion



A NONLINEAR CONGESTION NETWORK MODEL FOR PLANNING INTERNAL MOVEMENTS IN THE HAJJ

bу

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1.0 Introduction

The purpose of this paper is to identify issues in the Hajj internal transportation network and model the situation in order to draw general policy decisions in management of this unique situation. The most important constraints in this case are the religious ones, since they define the transportation and the movement of the people from one place to another. Any model must reflect these constraints in order to be implementable. These religious constraints are represented as time and space constraints. A temporal capacitated network is developed to represent the situation, with the objective to minimize congestion of traffic on roads and overcrowding of the holy places. This objective is chosen to enable the visitors to perform their duties as easily as possible.

In section 2 we describe the Hajj situation briefly, and in section 3 we identify issues to be considered in the modeling process. In section 4 we develop a linear network model, and in section 5 we present a numerical example for the Hajj situation. In section 6 we extend the model to a non-linear model to properly account for congestion via a non-linear function and we draw conclusions.

2.0 Description of the Hajj

The Hajj is an annual meeting for about two million Muslims to achieve one of the five pillars of Islam. The Hajj involves several visitations to several holy sites and it occurs every 354 days, since it is dated by the Islamic Lunar year. The Hajj process in this paper will be divided into three

phases. Phase one mainly consists of air and sea transportation of foreign population to Jeddah, and also inland transportation of foreign and native population. The duration of this phase is up to the eighth of the last month of the Lunar year, by that time all the pilgrims have gathered in one of the following towns: Jeddah, Makkah, Muna or Medina.

Phase two starts from the morning of the eighth of the last month in the Lunar year up to the end of the Hajj and the arrival of the pilgrims at the ports to leave for home. This phase includes part of the in-land transportation from Jeddah and Medina to Makkah and all the movement between the holy sites up to the completion of the Hajj. Its duration is roughly up to the nineteenth or the twentieth of the month. Phase three consists partly of the transportation between Makkah and the ports. It also includes the departure of all prilgrims for home. In this paper we deal with phase two, the "internal transportation network of the intramovement of the pilgrims", which constitutes the logistics of the religious process.

2.1 Phase Two of the Hajj

In general, the Hajj season begins at the start of the tenth month of the Muslim lunar calendar year and ends about the twentieth of the Dihu'L-Hijjah (the twelfth and final month of the lunar year). Most of the pilgrims arrive in the last fifteen days of the season. According the our model, phase two starts the morning of the eighth day of the last month of the lunar calendar year. By this time all pilgrims have already arrived in Saudi Arabia and they are either at Makkah, Muna, Jeddah or Medina (see dagram in Figure I).

It is a ritual that before arriving at Makkah every pilgrim has to wear the garment of iharm (restriction), is forbidden to hunt, argue, cut his hair, clip his nails or engage in any sexual activities. Also on arrival at

Makkah (45 miles east of Jeddah) each pilgrim has to make the greeting tawaf, the prescribed seven counterclockwise circumambulations of the Kaaba (a black room in the center of the holy mosque built by the prophet Ibraham). With the tawaf they perform the Sa'y--making seven trips between the hills of Safa nad Marwah. The path of Sa'y is enclosed in a long gallery which is part of the holy mosque.

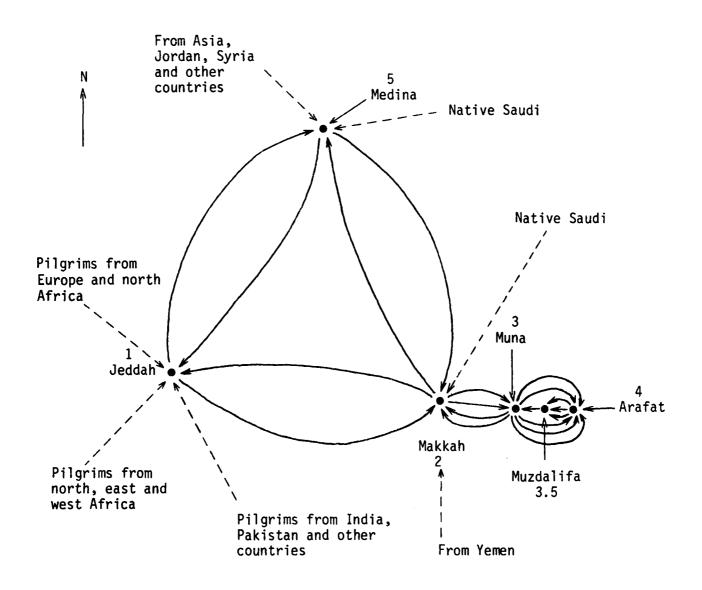
Also on the eighth day, those pilgrims who are not already in Muna, four miles east of Makkah, move through Makkah to Muan for the essential final days of the Hajj. The next day (on the ninth) everybody has to be in Arafat, eight miles east of Muna, to perform the <u>Standing</u>, the central ritual of the Hajj. The duration of the Standing is from noon of the ninth until sunset.

On the eve of the tenth, the pilgrims leave Arafat and stop at Muzdalifa, a place between Muna and Arafat. At Muzdalifa they collect pebbles to throw at the three "Satan's stoning points" in Muna during the following days. These points symbolize the force of evil. Those who leave for Makkah start doing one of the pillars of the Hajj Tawaf El ifada, the post-Arafat tawaf done in the same manner as the greeting tawaf. After finishing this tawaf pilgrims can put off iharm (restriction) and return to Muna to finish the Stoning of the devil. After finishing the Stoning, the Hajj is complete.

All pilgrims after the Hajj perform a farewell tawaf and some of them leave for Medina to visit the prophet's grave. Visiting Medina can be done before the Hajj starts and those who did it before the Hajj leave via Jeddah or by inland routes for home. Figure 1 shows all the holy sites and the routes of the pilgrims' movements.

Figure 1

A Diagram for the Islamic Holy Sites and the Flow of Pilgrims



- The solid lines represent the internal movement
- ----> The broken lines represent the external movement for coming to Hajj and leaving

3.0 Issues to be Considered in the Model

The most important elements here are the timing and place of each of the holy practices. This determines the flow of people from one place to another. We notice from section two that there is some flexibility in the timing of most of the pillars of the Hajj. The model must be able to take full advantage of that in order to make the Hajj as smooth as possible.

When the pilgrims travel to Makkah they are in large numbers and there is overcrowding of the roads which lead to Jakkah. On arrival at Makkah they perform the greeting tawaf. There they need some scheduling to ease overcrowding at the Kaaba.

The central ritual of the Hajj is the Standing at Arafat. This is a large place and can take all the pilgrims, but on the way to and from Arafat the big crunch occurs. Then the people shuttle between Makkah and Muna until they finish their Hajj.

In scheduling events in the Hajj, the following must be noted. First, the greeting tawaf can be done any time before the morning of the ninth of the Hajj month. The post-Arafat tawaf can be performed at any time from the eve of the tenth to the evening of the twelfth of the Hajj month, but most people like to do it earlier to finish their Hajj. Secondly, the Stoning of the Satan is flexible within two or three days, i.e., from the tenth up to the twelfth of the Hajj month. Third, the Sacrifice of the sheep can be done any time from the morning of the tenth until the evening of the twelfth, but most people do it on the tenth. Fourth, most people catch the 'Id prayer at the Sacred Mosque on the morning of the tenth. Fifth, the farewell tawaf can be done any time before leaving Makkah. Sixth, the visitation to Medina can be done before or after the Hajj and there are no time constraints on it.

The model should take advantage of the flexibility in the timing of the Hajj rituals, but also should allow room for pilgrims' preferences in choosing the time to do rituals if the models' specifications are to have any chance of being implemented.

4.0 Statement of the Model

4.1. The Constraints Set

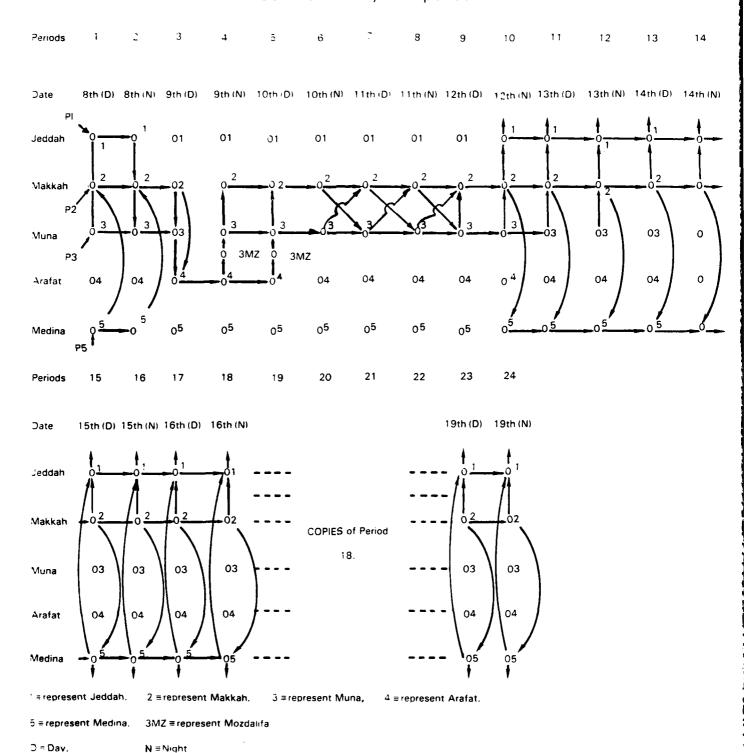
The following constraints set of the Hajj internal movement is shown in Figure 2. Figure 2 represents movements of pilgrims by half-days from the eighth of the Hajj month till the nineteenth. Each half a day is considered as a period, so the model consists of twenty-four periods. We think half a day is a reasonable period for general policy decisions, but for close monitoring of the pilgrims' movements the model can be represented in terms of shorter periods, i.e., in terms of one hour period. This will expand the model, but since the model is of network type, it can be solved easily.

Figure 2 gives a complete representation of the Hajj internal movements. There are two sets of arcs in Figure 2, one set represents movement of pilgrims within periods, the other set represents pilgrims who are staying in the same town for the next period.

The upper bounds on the arcs in the model should be considered very closely and the following considerations would be very useful:

- (1) the time of the period evening or morning,
- (2) the lodging capacity of each town,
- (3) the food and public facilities of each location,
- (4) the health facilities,
- (5) the availability of buses, cars, between any two towns on each route, and
 - (6) the timing of each ritual.

NETWORK REPRESENTATION For THE HAJJ Internal MOVEMENT Each Half A day is A period



Let

x_{ij}(t) = number of pilgrims going from location i to location j in
 period t;

 $y_{ij}(t,t+1)$ = number of pilgrims going from location i to location j during period t;

 $y_{ij}(t,t+1)$ = number of pilgrims staying at location i during period t; [In this case we do not consider in detail cross travel between riods from one site to another, since one-half day is more than sufficent travel time between any two sites; therefore, flexibility in the timing or rituals enables the model to accommodate cross travel.]

the maximum number of pilgrims who can travel easily at
day times from location i to location j, i.e., this is
the capacity of route (i,j)

the maximum number of pilgrims who can travel easily at
night time on route (i,j)

L; = lodging capacity of town i,

 K_{i} = food capacity of town i,

 b_i = the minimum of the public facilities' capacities at town i. Let 1 be Jeddah, 2 be Makkah, 3 be Muna, 3.5 be Muzdalifa , 4 be Arafat, and 5 be Medina.

P_i = number of pilgrims at town i at the beginning of the first period.

The following are the equations defined by the network in Figure 2. The numbers to the left of the equations represent the period and the node, i.e., 1.5 represent the equation for period one at node 5, or the equation for

period one at Medina and so on. Note that the equations $y_{ii}(t,t+1)$ is written as $y_i(t,t+1)$.

The arrow means the equations are completed on the next page.

	$x_{12}(1)$	x ₂₃ (1)	x ₅₂ (1)	$y_1(1,2)$	$y_2^{(1,2)}$	$y_3(1,2)$	y ₅ (1,2)	× ₁₂ (2) ,	^x 23 ^{(2) x} 52	(2)	$x_{12}(1) x_{23}(1) x_{52}(1) y_1(1,2) y_2(1,2) y_3(1,2) y_5(1,2) x_{12}(2) x_{23}(2) x_{52}(2) y_1(2,3) y_2(2,3) y_3(2,3) y_5(2,3)$,3) y ₃ (2,3)	y ₅ (2,	3)
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3.2											-1			+
3.3												-1		+
3.4														+
3.5													7	+

Equations for period 3, 4 and part of period 5. Notice period 3 has some variables on the previous period

	x ₂₃ (3)) × ₂₄ (3)	x ₃₄ (3)	y ₂ (3,4)	y ₃ (3,4)	y ₄ (3,4)	x ₃₂ (4) x	$x_{23}(3) x_{24}(3) x_{34}(3) y_2(3,4) y_3(3,4) y_4(3,4) x_{32}(4) x_4 3.5(4) x_3.5 3(4) y_2(4,5) y_3(4,5) y_3.5(4,5) y_4(4,5)$	5 3(4)	y ₂ (4,5)	y ₃ (4,5) y	3.5(4.5)	y ₄ (4,5)	_
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Part of the equations of period 5 and completion of these equations is on the next page.

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Constraints set for period 7, 8 and part of period 9:

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	323(7,8)	$y_{23}(7,8)$ $y_{32}(7,8)$ $y_{2}(7,8)$	y ₂ (7,8)	y ₃ (7,8)	y ₂₃ (8,9)	y ₃₂ (8,9)	y ₂ (8,9)	y ₃ (8,9)	<u> </u>
7.1									0
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7.4									0
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	×32(9)	y ₂ (9,10)	$y_3(9,10)$	$x_{21}^{(10)}$	× ₃₂ (10)	× ₂₅ (10)	$y_1(10,11)$		y ₃ (10,11)	y ₅ (10,11)	
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10.5						7				-	0
	Part of	the constra	int set for	period 11	and its co	ompletion	Part of the constraint set for period 11 and its completion is on the next page.	xt page.			
11.1							7			·	
11.2								-		·	
11.3									-	·	
11.4										·	
11.5										7	

Equations for period 11, 12 and part of those for period 13:

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Completion	of the	equations	Completion of the equations for period		13 is on the next page.								
									-1			7	†
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											7	7	+

Equations for periods 13, 14 and part of those for period 15:

	x ₂₁ (13)	x ₂₅ (13)	y ₁ (13,14)	y ₂ (13,14)	$x_{21}(13)$ $x_{25}(13)$ $y_{1}(13.14)$ $y_{2}(13.14)$ $y_{5}(13.14)$ $x_{21}(14)$ $x_{25}(14)$ $y_{1}(14.15)$ $y_{2}(14.15)$ $y_{5}(14.15)$	x ₂₁ (14)	x ₂₅ (14)	y ₁ (14,15)	y ₂ (14,15)	y ₅ (14,15)	
13.1	7		-								"
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	Completi	on of the	equations f	or period 1	Completion of the equations for period 15 is on the next page.	next page.					
15.1								۲.			†
15.2									-		+
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15.4											Ť
15.5										-1	+

Equations for period 15, 16 and part of those for period 17:

	x ₂₁ (15)		y ₁ (15,16)	y ₂ (15,16)	y ₅ (15,16)	x ₂₁ (16)	× ₂₅ (16))	$x_{25}(15)$ $y_1(15,16)$ $y_2(15,16)$ $y_5(15,16)$ $x_{21}(16)$ $x_{25}(16)$ $x_{52}(16)$ $x_{51}(16)$ $y_1(16,17)$ $y_2(16,17)$ $y_5(16,17)$	16)	y ₁ (16,17) y ₂	, (16,17)	(16,17)	
15.1	7		1										0 =
15.2	7			1									0 =
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15.4													0 =
15.5		7			1								0 =
16.1			-1			7		•	-1				0 =
16.2				7		-	-	7					0 =
16.3													0 =
16.4													0 =
16.5					-		-1					-	0 =
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x ₅₂ (18)							7			-
x ₅₁ (18)										-
x ₂₅ (18)										7
× ₂₁ (18)							-1			
y ₅ (17,18)					1					7
y ₂ (17,18)		-					-1			
y ₁ (17,18)	-					-1				
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× ₅₂ (17)		7			-					
x ₂₅ (17)		1			7					
x ₂₁ (17)	-1	1								
	17.1	17.2	17.3	17.4	17.5	18.1	18.2	18.3	18.4	18.5

The following periods 19, 20 up to 24 have the same pattern or structure as 18 so we will have just copies of the equations in 18. The following are the capacity constraints on the routes and the holy places.

$$0 \le x_{ij}(t) \le K_{ij}$$
 if t is odd
 $0 \le x_{ij}(t) \le L_{ij}$ if t is even

$$0 \le y_{i,j} (t,t+1) \le L_{i,j}$$

4.2. Objective Function

One of the objectives to be considered is space and routes utilization. The objective is of goal type to ease crowding as much as possible, i.e.

(4.2.1)
$$\text{Max} \sum_{i} |\min (K_{i}, L_{i}, b_{i}) - y_{ii}(t, t+1)| + \sum_{t} \sum_{ij} |K_{ij} - x_{ij}(t)|$$

$$+ \sum_{t} \sum_{ij} |L_{ij} - x_{ij}(t)| + \sum_{t} \sum_{ij} |L_{ij} - y_{ij}(t, t+1)|$$

$$\text{even}$$

Maximizing this function alone will allow for overcrowding of holy sites and we will be maximizing a convex function, but with the capacity constraints

$$\begin{aligned} &x_{ij}(t)\leqslant L_{ij} &, &x_{ij}(t)\leqslant K_{ij} & \text{and} \\ &y_{i\uparrow}(t,t+1)\leqslant \min(K_i,L_i,b_i) &, &y_{ij}(t,t+1)\leqslant L_{ij} \end{aligned}$$

that will not happen and the objective function will be transformed into the following equivalent linear function.

(4.2.2)
$$\min \sum_{t=1}^{\infty} y_{ij}(t,t+1) + \sum_{t=1}^{\infty} \sum_{ij} x_{ij}(t) + \sum_{t=1}^{\infty} \sum_{ij=1}^{\infty} y_{ij}(t,t+1)$$

Hence the model for the Hajj internal movement will minimize the linear function in (4.2.2) subject to all the constraints in section 4.1.

The above model could be updated if conditions on the routes and the holy sites are changed. It could be formulated in terms of shorter periods, for example on an hourly basis, if detailed monitoring of the Hajj internal movement is needed.

Another objective function to be considered is

$$\begin{aligned} \min \sum_{t} \sum_{i=1}^{n} |\min(K_{i}, L_{i}, b_{i}) - y_{i}(t, t+1)| &+ \sum_{t} \sum_{ij} |K_{ij} - x_{ij}(t)| \\ &+ \sum_{t} \sum_{ij} |L_{ij} - x_{ij}(t)| + \sum_{t} \sum_{ij} |L_{ij} - y_{ij}(t, t+1)| \end{aligned}$$

This is another type of a goal type objective and this with the constraints in section 4.1 can be transformed into a larger pure network.

Other objectives and constraints may also need consideration, e.g., the role of individual contractors ("Mutwafeen") may need more explicit consideration.

5.0 Examples and Extensions

The following example is a reasonable representation for the Hajj situation in the year 1980. The example was constructed using [4], a study done by the Hajj Research Center at Jeddah. Using this study and some personal judgement, the following data on routes and town capacities were specified.

Routes	<u>Day</u>	Night
Jeddah to Makkah	0 to 200,000	0 to 150,000
Makkah to Muna	0 to 500,000	0 to 400,000
Makkah to Medina	0 to 200,000	0 to 150,000
Makkah to Arafat	0 to 900,000	0 to 700,000
Muna to Arafat	0 to 800,000	0 to 700,000
Muna to Makkah	0 to 250,000	0 to 200,000
Medina to Makkah	0 to 100,000*	0 to 150,000

^{*}when 2-way traffic

Capacity Of	No. of Pilgrims
Jeddah	300,000
Makkah	1,000,000
Muna	600,000
Arafat	2,000,000
Medina	1,000,000

$$P_1 = 200,000$$
; $P_2 = 800,000$; $P_3 = 400,000$; $P_5 = 200,000$; $P_4 = 0$

The above example, with some variations to allow for pilgrim increase, was solved in order to evaluate the model and its representation of the real situation. To achieve this evaluation, the dual variables of the model were utilized. The dual variables give an evaluation of the model response to traffic volumes and routes capacities.

In all three examples the dual evaluations point to the route Mina to Mecca at period four as pre-eminent in relief of congestion since it was the most negative dual variable. An increase in the capacity of this route by one unit will result in 127 units reduction in the objective function (which increases congestion) since the value of its dual variable is -127. The examples further show that major concern should be given to the Hajj internal movement in period four and five. The complete solution of this example is in Table 1 in the Appendix.

The other negative dual variables occur for the routes Jeddah to the Sink and Medina to the Sink. The most negative dual variable is associated with the capacity of the route Jeddah to the Sink of value -14. That means an improvement in Jeddah port capacity of one unit will result in a reduction of 14 units in the objective function. Using the magnitude of the dual

variables, the ports can be ranked in terms of their importance in reducing traffic congestion. The Jeddah port is the most important to the Hajj internal movement and Medina is next.

The second and the third examples give directions where improvement should be made in case the number of pilgrims increase. Both examples show that the Jeddah-Mecca route must be improved to increase its capacity to handle the anticipated increase in pilgrims in the future.

These examples give some insight into decision making for Hajj scheduling but the simple objective function does not reflect very well all the possible effects of levels of congestion on different routes. Hence, they give scheduling plans which are insensitive to routes and to changes in capacity. A more appropriate measure of congestion, which will result in better distributions of traffic between the routes, is needed.

Such a measure of congestion will be presented in the next section. It results in a non-linear objective function network. We solve it by piecewise linearization and shall compare its results with those of this model.

6.0 Non-Linear Network for the Hajj Internal Movement

In the previous section we examined a linear model for the Hajj Internal Movement. The linear objective is not an appropriate measure of congestion, since it does not correctly reflect the fact that rate of congestion increases with increases in closeness to capacity on a route segment. In this section we introduce a non-linear measure of congestion for each route which depends on the capacity of the route segment and the density of traffic on it. In the next section we will elaborate on the properties of this measure.

Let $R_{ij}(x_{ij}(t))$ and $\overline{R}_{ij}(y_{ij}(t,t+1))$ be convex non-linear functions which measure the congestion on arcs $x_{ij}(t)$ and $y_{ij}(t,t+1)$. The model in section 4.2 is now altered (only in the objective function) to be

(6.0.1) Min
$$\sum_{t=1}^{24} \sum_{ij} R_{ij}(x_{ij}(t)) + \sum_{t=1}^{24} \sum_{ij} \overline{R}_{ij}(y_{ij}(t,t+1))$$

subject to
$$\sum_{j=1}^{5} \epsilon_{ij} x_{ij}(t) + \sum_{j} \epsilon_{ij}(t) y_{ij}(t,t+1) = 0$$

$$i = 1,2,...,5$$
; $t = 1,2,...,24$; $x_{i,i}(t), y_i(t,t+1) \ge 0$

where the incidence numbers ε_{ij} are 1, -1, or zero. The model in (6.0.1) can be replaced by the following capacitated linear model wherein we have approximated the $R_{ij}(x_{ij}(t))$ and $R_{ij}(y_{ij}(t,t+1))$ functions by two linear segments. In the next section we shall develop a method for choosing the two line segments. Employing such an approximation (6.0.1) becomes

(6.0.2) Min
$$\sum_{t=1}^{24} \sum_{i=1}^{5} \sum_{k=1}^{5} \sum_{k=1}^{2} R_{ijk} x_{ijk}(t) + \sum_{t=1}^{5} \sum_{i=1}^{5} \sum_{k=1}^{2} \overline{R}_{ijk} y_{ijk}(t)$$

subject to
$$\sum_{j}^{24} \sum_{k=i,j}^{2} \varepsilon_{i,j} x_{i,j,k}(t) + \sum_{j}^{5} \sum_{k=i,j}^{2} (t) y_{i,j,k}(t,t+1) = 0$$

$$i = 1,2,...,5$$
; $0 \le x_{ijk}(t) \le \Delta_{ijk}$; $0 \le y_{ijk}(t) \le \Delta_{ijk}$

The dual of (6.0.2) is

$$\text{Max} \sum_{t=1}^{24} \sum_{i}^{5} \phi_{i}(t) \cdot 0 - \sum_{t=1}^{24} \sum_{i}^{5} \sum_{j}^{5} \sum_{k}^{2} \psi_{ijk}(t) \Delta_{ijk} - \sum_{t=1}^{24} \sum_{i}^{5} \sum_{j}^{5} \sum_{k}^{2} w_{ijk}(t) \overline{\Delta}_{ijk}$$

subject to

$$\begin{split} &\sum_{i} \epsilon_{ij} ^{\varphi_{i}(t)} - \Psi_{ijk}(t) \leqslant R_{ijk} \\ &\sum_{i} \epsilon_{ij} ^{\varphi_{i}(t)} - W_{ijk} \leqslant R_{ijk} \ \forall \ j, \ t, \ \text{where} \ \Phi_{i} \ \text{unrestricted}, \ W_{ijk}, \ \Psi_{ijk} \geqslant 0. \end{split}$$

In an optimal solution to (6.0.2) the dual variables Φ^*_i , w^*_{ijk} and Ψ^*_{ijk} provide evaluators for the initial points at which changes in "resistance" to traffic volumes occurs. Hence a means is provided for evaluating possible changes associated with those features of the network in terms of their effects on the resulting traffic volumes at the times associated with the movements.

To develop (6.0.2) we nedd the R $_{ijk}$, $\bar{\Delta}_{ijk}$ for the model. The next section will elaborate on the congestion measure we have chosen and on how the R $_{ijk}$, $\bar{\Delta}_{ijk}$ and Δ_{ijk} are determined.

6.1 A Convex Non-linear Measure of Traffic Congestion

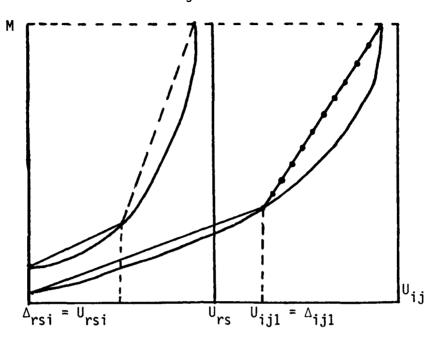
The measure of Congestion of traffic should:

- 1) increase with increase in traffic flow,
- have an increasing rate of increase with traffic flow increase (i.e. be a convex function),
 - 3) be zero or very close to zero at zero flow,
- 4) approach infinity when flow approaches the capacity of the route.One such measure of traffic congestion is

(6.1.1)
$$f(x_{ij}) = \frac{1}{U_{ij} - x_{ij}}$$

where U_{ij} is the capacity of the route movement (i,j,). To apply (6.0.2) we need to find R_{ijk} and Δ_{ijk} and what the relationships are between these Δ_{ijk} and R_{ijk} . Thus we break the non-linear function into two line segments. In order to exhibit further relationships, in figure 6-1 we exhibit simultaneously two examples.





For any given two routes (i,j) and (r,s), they have the measures of congestion $R_{ij}(x_{ij})$ and $R_{rs}(x_{rs})$. We break the function $R_{ij}(x_{ij})$ into two line segments. The first line segment is the line that joins the two points $\left(0,\frac{1}{U_{ij}}\right)$ and $\left(\frac{1}{U_{ij1}},\frac{1}{U_{ij}-U_{ij1}}\right)$. We now show how from determination of the breakpoint for one route (i,j), we can simultaneously determine the breakpoints for all other routes (r,s). Using the concept that congestion will be the same if traffic density relative to route capacity is the same, we consider

$$\frac{x}{U_{ij}} = \frac{y}{U_{rs}}$$

where x is the flow in route (i,j) and y is the traffic flow in route (r,s). Using (6.1.2) we have

$$\frac{U_{rs1}}{U_{rs}} = \frac{U_{ij1}}{U_{ij}}$$

then

$$U_{rs\bar{1}} = \left(\frac{U_{rs}}{U_{ij}}\right)U_{ij1}$$

Thus the breakpoints are determined immediately by the route capacity and so are the slopes for all the routes.

(6.1.5) The
$$R_{rs1} = \left(\frac{1}{U_{rs}-U_{rs1}} - \frac{1}{U_{rs}}\right) \div U_{rs1}$$

6.1.1 THEOREM

If R_{ijl} is the slope of the first line segment for $R_{ij}(x_{ij})$, then

$$R_{rs1} = \frac{U^2_{ij}}{U^2_{rs}} \cdot R_{ij1}$$

for all (r,s).

Proof:
$$R_{rs}(x_{rs}) = \frac{1}{U_{rs}^{-x}_{rs}}$$

 R_{rs1} is the slope of the line joining $\left(0,\frac{1}{U_{rs}}\right)$ and $\left(U_{rs1},\frac{1}{U_{rs}-U_{rs1}}\right)$

$$R_{rs1} = \left(\frac{1}{U_{rs}^{-U}_{rs1}} - \frac{1}{U_{rs}}\right) \div U_{rs1}$$

$$= \frac{U_{rs}^{-U}_{rs1} + U_{rs1}}{U_{rs1} \left(U_{rs}^{-U}_{rs1}\right) U_{rs}} = \frac{1}{U_{rs} \left(U_{rs}^{-U}_{rs1}\right)}$$

$$v_{rs1} = \frac{v_{rs}}{v_{ij}} v_{ij1}.$$

Hence

$$R_{rs1} = \frac{1}{U_{rs} \left(U_{rs} - \frac{U_{rs}}{U_{ij}} U_{ij1}\right)} = \frac{1}{\frac{U^{2}_{rs}}{U_{ij}}} \left(U_{ij} - U_{ij1}\right)$$

$$= \left(\frac{U^{2}_{ij}}{U^{2}_{rs}}\right) \frac{1}{U_{ij} \left(U_{ij} - U_{ij1}\right)} = \frac{U^{2}_{ij}}{U^{2}_{rs}} R_{ij1}$$

$$Q \cdot E \cdot D$$

To determine the second line segment slope, let

$$M = \frac{1}{U_{ij} - x^*_{ij}}$$
 where
$$U_{ij} - x^*_{ij} = n$$
 for all (i,j). Then
$$R_{ij2} = \frac{M - \frac{1}{U_{ij} - U_{ij1}}}{x^*_{ij} - U_{ij1}}$$

Computing R_{ijk} , Δ_{ijk} for all functions on the routes, putting them and their associated variables into (6.0.2), we abtain a linear network. This model has been applied to the Hajj Internal Movement using the same data as in the linear case, and solved.

6.2 Results and Conclusions

The non-linear measure of traffic congestion is applied to the same example previously solved for the linear case. All the necessary piece-wise linearization is performed as described in section 6.1. The

optimal solution for the non-linear case depicts the Hajj situation in more realistic terms by picking up the required movements between Muna and Makkah in periods 5, 6, and 7 without imposing lower bounds on traffic movements on routes.

Moreover we see that the evaluation given by the dual variables for the non-linear case give a clear indication of routes which might ease traffic congestion.

The model shows that the time interval of concern for the Hajj Internal Movement is from period four to period seven. To comprehend the ways of easing the traffic congestion there we need to concentrate on the Hajj Internal Movement from period three to period eight and use the results of this model as a guide for traffic improvements.

The model evaluators clearly signal the following routes as the key routes in easing the traffic congestion. The route with the most negative dual variable is Muna to Makkah in period four. The second route is Muna to Makkah at period 5, followed by Muna to Muna between periods five and six.

The model shows that the pilgrims' time of departure depends strictly on the capacity of the ports. Upgrading the capacities of the ports will help in smoothing the Hajj process. Another important way to ease the traffic congestion is to divide the pilgrims into two groups: one to visit Medina prior to the Hajj, the other after the Hajj. Then the group which visits Medina after the Hajj departs from Medina. This will ease the traffic after the Hajj.

Complete optimal solutions for the linear and the non-linear cases are shown in Tables 1 and 2 in the appendix. The optimal solution

includes the optimal traffic flow, the upper bound on each arc, the "cost" of each arc in terms of resistance to traffic and the dual evaluators.

 $\begin{tabular}{ll} TABLE 1 \\ \hline \begin{tabular}{ll} Optimal Solution for the Linear Example \\ \end{tabular}$

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 $$\operatorname{TABLE}\ 2$$ Optimal Solution for the Non-linear Example

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20. ABSTRACT (Continue on reverse side if necessary an	d identify by block number)											
This paper develops a non-1	inear dynamic cap	pacitated network model for										
planning the movements of pilg	rims in the Hajj	, one of the world's largest										
mass movements, according to r	eligious ritual,	which would assist in min-										
imizing traffic congestion and	the overcrowding	g of the holy sites. A new										
non-linear representation of c	ongestion with c	onvenient mathematical pro-										
perties is made. The model is												
qualitative background for gen	eral policy deci	sions on the Hajj transpor-										
tation.												

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